

## **SOLAPUR UNIVERSITY, SOLAPUR**



### **SYLLABUS**

### **FOR**

### **M.Sc. (Part-I) MATHEMATICS (Semester I and II) Choice Based Credit System (CBCS)**

**WITH EFFECT FROM ACADEMIC YEAR 2016-17  
(JUNE-2016).**

**SOLAPUR UNIVERSITY, SOLAPUR**  
**SCHOOL OF COMPUTATIONAL SCIENCES**  
**DEPARTMENT OF MATHEMATICS**

**Revised Syllabi of M.Sc. in Mathematics (Choice Based Credit System)**

- 1) **Title of the course:** M.Sc. in Mathematics
- 2) **Pattern:** Semester and Credit system.
- 3) **Duration of Course:** 2 years
- 4) **Strength of the Students:** 40
- 5) **Eligibility:** For M. Sc. in Mathematics following candidates are eligible.
  - (i) B.Sc. with Mathematics as principal level.
  - (ii) B.Sc. with any subject as principal and Mathematics at subsidiary level.

M. Sc. program in Mathematics consists of 100 credits. Credits of a course are specified against the title of the course.

**A Four Semester M.Sc. Mathematics Course**

Semester	No. of Papers/ Practical's / Seminar	Marks	Credits
<b>Semester I</b>			
• Theory Papers	05	500	20
• Practical Papers	01	100	04
• Seminar/Tutorial/Home Assignment /Field Tour/ Industrial Visit	01	25	01
<b>Semester II</b>			
• Theory Papers	05	500	20
• Practical Papers	01	100	04
• Seminar/ Tutorial/Home Assignment /Field Tour/ Industrial Visit	01	25	01
<b>Semester III</b>			
• Theory papers	05	500	20
• Practical Papers	01	100	04
• Seminar/ Tutorial/Home Assignment /Field Tour/ Industrial Visit	01	25	01
<b>Semester IV</b>			
• Theory papers	05	500	20
• Practical Papers	01	100	04
• Seminar/ Tutorial/Home Assignment /Field Tour/ Industrial Visit	01	25	01
<b>Total marks and credits for M.Sc. Course</b>		<b>2500</b>	<b>100</b>

**Solapur University, Solapur****School of Computational Sciences****M.Sc. Mathematics Choice Based Credit System (CBCS)****Course Structure M.Sc. Part-I (Mathematics) w.e.f. June 2016-17**

<b>M.Sc. MATHEMATICS SEMESTER-I</b>								
<b>Paper Code</b>	<b>Title of the Paper</b>	<b>Semester Examination</b>			<b>L</b>	<b>T</b>	<b>P</b>	<b>Credits</b>
		<b>Theory</b>	<b>IA</b>	<b>Total</b>				
<b>Hard Core Theory</b>								
<b>HCT 1.1</b>	Algebra I	70	30	100	4	--	--	4
<b>HCT 1.2</b>	Real Analysis I	70	30	100	4	--	--	4
<b>HCT 1.3</b>	Differential Equations	70	30	100	4	--	--	4
<b>HCT 1.4</b>	Classical Mechanics	70	30	100	4	--	--	4
<b>Soft Core-Theory (Any one)</b>								
<b>SCT 1.1</b>	Number Theory	70	30	100	4	--	--	4
<b>SCT 1.2</b>	Object Oriented Programming using C++							
<b>Practical</b>								
<b>HCP1.1</b>	Practical 1 ( Practical based on HCT 1.1, HCT1.2, HCT1.3)	35	15	50	--	--	4	2
<b>HCP1.2</b>	Practical 2 (Practical based on HCT 1.4, SCT)	35	15	50	--	--	4	2
	Seminar/Tutorial/ Industrial Visit/ Field Tour	---	25	25	--	1	--	1
<b>Total for Semester-I</b>		<b>420</b>	<b>205</b>	<b>625</b>	<b>--</b>	<b>--</b>	<b>--</b>	<b>25</b>
<b>M.Sc. MATHEMATICS SEMESTER-II</b>								
<b>Code</b>	<b>Title of the Paper</b>	<b>Semester Examination</b>			<b>L</b>	<b>T</b>	<b>P</b>	<b>Credits</b>
		<b>Theory</b>	<b>IA</b>	<b>Total</b>				
<b>Hard Core Theory</b>								
<b>HCT 2.1</b>	Algebra II	70	30	100	4	-	--	4
<b>HCT 2.2</b>	Real Analysis II	70	30	100	4	-	--	4
<b>HCT 2.3</b>	General Topology	70	30	100	4	-	--	4
<b>Soft Core Theory (Any One)</b>								
<b>SCT 2.1</b>	Complex Analysis	70	30	100	4	-	--	4
<b>SCT 2.2</b>	Relativistic Mechanics							
<b>Open Elective Theory (Any one)</b>								
<b>OET 2.1</b>	Fundamentals in Mathematics	70	30	100	4	-	--	4
<b>OET 2.2</b>	Vedic Mathematics							
<b>Practical (Hard and Soft core)</b>								
<b>HCP 2.1</b>	Practical 3 (Practical based on HCT 2.1,2.2,2.3 and SCT )	35	15	50	--	-	4	2
<b>Practical (Open Elective) Any One</b>								
<b>OEP 2.1</b>	Practical 4 (Practical based on OEP 2.1)	35	15	50	--	-	4	2
<b>OEP 2.2</b>	Practical 4 (Practical based on OEP 2.2)							
	Seminar/Tutorial/ Industrial Visit/ Field Tour	---	25	25	--	1	--	1
<b>Total for Semester-II</b>		<b>420</b>	<b>205</b>	<b>625</b>	<b>--</b>	<b>-</b>	<b>--</b>	<b>25</b>

### **Evaluation Scheme:**

Each theory paper will have 100 marks out of which 70 marks will be for Term End examination and 30 marks for Internal Assessment. The candidate has to appear for internal evaluation of 30 marks and external evaluation (University Examination) of 70 marks for each theory paper.

Each practical paper will have 50 marks out of which 35 marks will be for Term End examination and 15 marks for Internal Assessment. The candidate has to appear for internal evaluation of 15 marks and external evaluation (University Examination) of 35 marks for each practical paper.

### **Internal Evaluation:**

- In case of theory papers internal examinations will be conducted by department / school.
- In case of practical papers, 5 marks shall be for day-to-day journal and 10 marks shall be for internal test, which will be conducted by the department / school.

### **External Evaluation (End of Term University Examination):**

#### **I) Nature of Theory question paper:**

- 1) Each Theory paper is of 70 marks.
- 2) Each Theory paper will be of 2 hours and 30 minutes duration
- 3) There shall be 7 questions each carrying 14 marks.
- 4) Students have to attempt **five questions**.
- 5) Q.No.1 is **compulsory** and shall contain 14 objective type sub-questions each carrying 1 mark.
- 6) Q. No.2 is **compulsory** and shall contain 4 short answer type sub-questions each carrying 3 or 4 marks.
- 7) Students have to attempt **any three** questions from Q. NO. 3 to Q. No. 7.
- 8) Q. NO. 3 to Q. No. 7 shall contain 2 long answer type sub-questions.

#### **II) Nature of Practical question paper: (End of Term Examination)**

**For Sem-I and II:** Practical examination will be conducted for 30 marks and is of two hours duration. There shall be 05 questions each of 10 marks, of which student has to attempt any 03 questions. VIVA will be for 5 marks.

**Paper no. I**

**Paper Code: HCT1.1**

**Algebra - I**

**UNIT I:** Groups (15 L)

Commutator subgroups, P- Subgroups, Conjugate classes, Zassenhaus lemma, G- sets, class equation, Sylow theorems

**UNIT II:** (15 L)

Normal and subnormal series, Composition series, Jordan -Holder Theorem, Solvable groups, Nilpotent groups.

**UNIT III:** (15 L)

UFD, PID, Euclidean domain, arithmetic in Euclidean domains

**UNIT IV:** Polynomial rings, (15 L)

Polynomial ring over the rational field, The Eisenstein criteria, Division algorithm, irreducible polynomials, ideal structure in  $F[X]$ , Uniqueness of factorization in  $F[x]$ , UFD in Polynomial rings, Modules, Submodules.

**Recommended Books:**

1. I.N.Herstein . Topics in Algebra. Wiley Eastern Ltd. New Delhi 1975.
2. J. B. Fraleigh, Basic Algebra, Narosa pub.
3. Joseph A. Gallian, Contemporary Abstract Algebra, Narosa Pub.

**Books for Reference :**

1. P.B.Bhattacharya, S.K.Jain and S.R. Nagpaul. Basic Abstract Algebra (2nd Edition) Cambridge University, Press Indian Edition 1997.
2. M. Artin Algebra, Prentice-Hall of India 1991
3. N.Jacobson, Basic Algebra Vols I and II Freeman 1988 ( Kalse Published by Firmcstan Publishing Company.)
4. S.Lang Algebra 3rd edition. Addison-Westely 1993
5. O.S. Luther and I.B.S. Passi, Algebra Vol. I-Groups. Vol. II-Rings, Narosa Publishing House (Vol 1-1996 Vol. II 1- 1999)
6. D.S.Malik & N.Mordeson and M.K.Sen Fundametnals of Abstract Algebra, Mc. Graw Hill International Edition, 1997.

## Paper No. II

### Paper Code: HCT 1.2

#### Real Analysis – I

**UNIT I:** Riemann Integration :- [1] (15 L)

Definition and existence of the integral, Refinement of partitions, Darboux's theorem, Conditions of integrability, Integrability of the Sum and difference of integrable functions, The integral as a limit of sums, Some integrable functions, Integration and differentiation, the fundamental theorem of Calculus, Mean Value theorem of integral Calculus, Second Mean Value theorem.

**UNIT II** Riemann – Stieltjes integral [1] :- (10 L)

Definition and existence of the integral, A condition of integrability

**UNIT III** Multivariable differential calculus : [2] (20L)

Introduction, the directional derivative, Directional derivatives and continuity, total derivative, the total derivative expressed in terms of partial derivatives, the Jacobian matrix , the chain rule, the mean value theorem, for differentiable functions, Taylors formula for functions from  $\mathbb{R}^n$  to  $\mathbb{R}^1$

**UNIT IV** Implicit functions and Extremum problems . [ 2,3] (15 L)

Functions with nonzero Jacobian determinant, The inverse function theorem, The Implicit function theorem, Extrema of real valued functions of one variable.

#### Recommended Books :-

- 1) Mathematical Analysis, 2<sup>nd</sup> ed., S. C. Malik and Savita Arora, New Age international ltd.
- 2) Apostol T. M. Mathematical Analysis , ( 2<sup>nd</sup> edition ) 12.1 – 12.5 , 12.8, 12.9, 12.11, 12.12, 12.14, 13.1, to 13.5 Narosa Pub.

#### Reference: Books :-

- 1]Burkill and Burkill A second course Mathematical Analysis, Cambridge University Press ( 1970 )
- 2]Walter Rudin,Principles of Mathematical Analysis(3<sup>rd</sup> Ed)MC Graw Hill
- 3] A Basic Course in Real Analysis , Ajit Kumar & S.Kumaresan, CRC press
- 4]Introduction to Real Analysis.Robert G.Bartle,Donald R,Sherbert, Wiley India Pvt ltd.

### **Paper No. III**

### **Paper Code: HCT 1.3**

### **Differential Equations**

**Unit I:** Linear Equations with constant coefficients: (20 L)

The second order homogeneous equation, initial value problems for second order equations, Linear dependence and independence. A formula for the Wronskian, the non-homogeneous equations of order two, the homogeneous equations of order n, initial value problems for the nth order equations, Equations with real constants, The non-homogeneous equation of order n

**Unit II:** Linear Equations with variable coefficients: (15 L)

Initial value problems for the homogeneous equations, solutions of the homogeneous equations, The Wronskian and linear independence, reduction of the order of a homogeneous equation, Homogeneous equations with analytic coefficients.

**Unit III:** Linear Equations with regular singular points: (15 L)

The Euler equations, second order equations with regular singular points, The Bessels equation.

**Unit IV:** Existence and uniqueness of solutions: (10 L)

The method of successive approximations, The Lipschitz condition.

#### **Recommended Books :**

1. An introduction to ordinary differential equations. by E.A. Coddington (1974) Prentice Hall of India Pvt.Ltd. New Delhi.

#### **Reference Books :**

1. Theory of ordinary differential equations by E.A. Coddington and Levinson (1955) McGraw Hill, New York

2. Elementary differential equations by E.D. Rainvills (1964) The Macmillan company, New York.

3. Ordinary Differential equations by G. Birkoff and G.G.Rota John Willey and Sons.

4. Differential Equations with Applications and Historical note by G.F. Simmons (1972) MacGraw Hill, Inc. New York.

5. Ordinary Differential Equations by Somasundaram, Narosa pub.

**Paper No. IV**  
**Paper Code: HCT 1.4**  
**Classical Mechanics**

**Unit-I :** ( 15 L)

Mechanics of a particle, Mechanics of a system of particles, constraints, Generalised coordinates, D'Alembert's principle, Lagrange's equations of motion, the forms of Lagrange's equation for velocity dependent potential, and dissipative forces, applications of Lagrangian formulation, cyclic co-ordinates and generalised momentum, conservation theorems.[1]

**Unit –II** ( 15L)

Functionals, basic lemma in calculus of variations, Euler- Lagrange's equations, the case of several dependent variables, the minimum surface of revolutions, the problem of Brachistochrone, Isoperimetric problems, Problem of the maximum enclosed area, shape of a hanging rope [2] [1].

**Unit –III** ( 15L)

Hamilton's principle, Lagrange's equations from Hamilton's principle, (holonomic system)Hamilton's equations of motion from a variational principle. The principle of least action cyclic coordinates and Routh's procedure, conservation theorems and physical significance of Hamiltonian [1]

**Unit –IV** ( 15 L)

The kinematics of rigid body motion, The independent co-ordinates of a rigid body, orthogonal transformations, properties of transformation matrix, infinitesimal rotations, the Eulerian angles, the Cayley-Klein parameters, Euler's theorem on motion of rigid body. Angular momentum and kinetic energy of motion of a rigid body about a point, [1].

**Recommended Books :**

1. Classical Mechanics by H.Goldstein (1980) Narosa Publishing House, New Delhi
2. Calculus of variations with applications to Physics and Engineering (International series in Pure and Applied Mathematics) by Robert Weinstock (1952) McGraw-Hill book comp. New York.
3. Classical Mechanics by N.C.Rana and P.S. Joag (1991) Tata McGraw Hill, New Delhi.

**Reference Books :**

1. A treatise on the Analytical Dynamics of Particles and rigid bodies. by E.T.Whittaker (1965) Cambridge University Press.
2. Classical Mechanics by E.A.Desolge, Vol. I and II (1982) John-Wiley and sons, New York.
3. Classical Mechanics A Modern Perspective by V.Barger and Martin Olsson(1995) McGraw Hill, Inc.New York.
4. Classical Machanics with introduction to Non-linear oscillation and chaos by V.B.Bhatia (1997) Narosa Pub.House
5. Classical Mechanics by J. C. Upadhyay, Himalaya Pub.



**Paper No.V**  
**Paper Code: SCT1.1**  
**Number Theory**

**Unit- I**

Review of divisibility, The division algorithm, Greatest common divisor , Euclidean algorithm Diophantine equation  $ax + by = C$ . Primes and their distribution , Fundamental Theorem of Arithmetic, The Goldback Conjecture. (15 L)

**Unit- II**

Congruences, Properties of Congruences, Linear congruences, Special divisibility tests. Fermats theorem, Fermats factorization method, Little theorem, Wilsons theorem. (15 L)

**Unit-III**

Number theoretic functions, The functions  $\tau$  and  $\sigma$ , The Mobius Inversion formula, The greatest integer function, Eulers Generalization of Fermats theorem Euler's phi function, Euler's theorem, properties of phi function. (15 L)

**Unit-IV**

Primitive roots, The order of an integer modulo  $n$ , primitive roots for primes, composite numbers having primitive roots, The theory of Indices. (15 L)

Recommended book:

1. D.M.Barton : Elementary Number Theory, Universal book stall, New Delhi.

Reference Books :

2. S.B.Malik : Basic Number theory Vikas publishing House.
3. George E.Andrews : Number theory, Hindusthan Pub. Corp.(1972)
4. Nisen Zuckerman : An Introduction to theory of numbers.
5. Hari Kishan : Number Theory , Pragati edition.
6. Pundir : Number Theory, Pragati edition.

**Paper No. V**  
**Paper Code: SCT:1.2**  
**OBJECT ORIENTED PROGRAMMING USING C++**

**Unit :1**

(A)Algorithm Development : Problem definition, Writing step by step procedure, representation in terms of Flow chart,, Tracing, Testing

(B)Overview Of C++ : Object Oriented Programming, Introducing C++ Classes, Concepts of Object Oriented Programming, C++ as a superset of C, New style comments, main function in C++, meaning of empty argument list, function prototyping, default arguments and argument matching, User defined data types: enumerated types, use of tag names, anonymous unions, scope of tag names.

(C)Classes & Objects :Classes, Structure & Classes, Union & Classes, Inline Function, Scope Resolution operator, Static Class Members: Static Data Member, Static Member Function, Passing Objects to Function, Returning Objects, Object Assignment. Friend Function, Friend Classes. **(12Lectures)**

**Unit:2**

(A)Array, Pointers References & The Dynamic Allocation Operators: Array of Objects, Pointers to Object, Type Checking C++ Pointers, The This Pointer, Pointer to Derived Types, Pointer to Class Members, References: Reference Parameter, call by reference and return by reference Passing References to Objects, Returning Reference, Independent Reference, C++'s Dynamic Allocation Operators, Initializing Allocated Memory, Allocating Array, Allocating Objects.

(B)Constructor & Destructor: Introduction, Constructor, access specifiers for constructors, and instantiation, Parameterized Constructor, Multiple Constructor in A Class, Constructor with Default Argument, Copy Constructor, Destructor.

(C)Overloading as polymorphism : Function & Operator Overloading : Function Overloading, Overloading Constructor Function Finding the Address of an Overloaded Function, Operator Overloading: Creating A Member Operator Function, Creating Prefix & Postfix Forms of the Increment & Decrement Operation, Overloading The Shorthand Operation (I.E. +=,-= Etc), Operator Overloading Restrictions, Operator Overloading Using Friend Function, Overloading New & Delete, Overloading Some Special Operators, Overloading[ ], ( ), -, Comma Operator.

**(15 Lectures)**

**Unit :3**

(A)Inheritance : Base Class Access Control, Inheritance & Protected Members, Protected Base Class Inheritance, Inheriting Multiple Base Classes, Constructors, Destructors & Inheritance, When Constructor & Destructor Function are Executed, Passing Parameters to Base Class Constructors, Granting Access, Virtual Base Classes .

(B)Virtual Functions & Polymorphism : Virtual Function, Pure Virtual Functions, Early Vs. Late Binding, Templates and Exception Handling.

(C) Templates: Reason for templates compactness and flexibility, function template examples explicit specialization, class templates, out of class definition of member functions **(15 Lectures)**

#### **Unit:4**

(A) The C++ I/O System Basics : C++ Streams, The Basic Stream Classes C++ Predefined Streams, Formatted I/O: Formatting Using The Ios Members, Setting The Format Flags, Clearing Format Flags, An Overloaded Form Of Setf ( ), Using Width() Precision() and Fill(), Using Manipulators to Format I/O, Creating Your own Manipulators

(B) Working with files : Introduction, Classes for file stream operations, Opening and Closing file, Open(): File Modes, File pointers and their Manipulations, Sequential Input and Output Operations, Updating a File: Random Access , Error Handling During File Operations  
(8 Lectures)

#### **Reference books:**

- 1) C++ The Complete Reference By *Herbert Schildt - Tmh*
- 2) C++ By *Balguruswami – Tata Mcgraw Hills*
- 3) C++ By M. Kumar, Tata Mcgraw

## Mathematics Practical Paper-1

Paper Code: HCP1.1

1. At least four practicals should be conducted on hard core theory paper HCT 1.1.
2. At least four practicals should be conducted on hard core theory paper HCT 1.2
3. At least four practicals should be conducted on soft core theory paper HCT 1.3

### Unit – I :- Algebra I

- 1) Problems on Isomorphism theorems & Sylow's Theorems.
- 2) Problems on Normal, Solvable & Nilpotent groups
- 3) Problems on UFD, PID, ED
- 4) Problems on Polynomial rings.

### Unit – II :- Real Analysis I

- 1) Problems on Riemann Integration.
- 2) Problems on Multivariable Calculus
- 3) Problems on Implicit functions
- 4) Problems on extremum Problems.

### Unit – III :- Differential Equations

- 1) Problems on Linear equations with constant coefficients
- 2) Problems on Linear equations with Variable coefficients.
- 3) Problems on Linear equations with regular singular points.
- 4) Problems on Method of successive approximation & Lipchitz condition.

Instruction : All practical's should be solved either by using C or C++ language.

## Mathematics Practical Paper-2

Paper Code: HCP1.2

1. At least four practicals should be conducted on hard core theory paper HCT 1.4
2. At least four practicals should be conducted on hard core theory paper SCT1.1/1.2

Instruction : All practical's should be solved either by using C or C++ language.

**Paper No. VI**

**Paper Code: HCT 2.1**

**Algebra - II**

**Unit –I** ( 20 L)

Introduction to Extension fields, field adjunctions, Algebraic and Transcendental elements, Simple extensions, Finite extensions, Algebraic extensions, Roots of Polynomials, Multiple roots, Splitting field, Uniqueness of Splitting field, Separable elements, Separable extensions, Perfect field.

**Unit II**

The elements of Galois theory, Automorphism of Fields, Fixed fields, Group of Automorphisms of a field K relative to subfield F of K, Normal extension, Galois group, Fundamental theorem of Galois theory. (15 L)

**Unit III**

Finite fields and its applications. (10 L)

**Unit IV**

Constructible real numbers, Solvability by radicals, Totally inseparable extensions, Cyclotomic extensions. (15 L)

**Recommended Books :**

- 1.Herstein I.N. : Topics in Algebra, Wiley Eastern Ltd.,Second ed. 1993.
- 2.J.B. Fraleigh : A first course in Abstract Algebra, Narosa Pub.Co.

**References :**

1. P.B.Bhattacharya, S.K.Jain and S.R. Nagpaul. Basic Abstract Algebra (2nd Edition) Cambridge University, Press Indian Edition 1997.
2. M.Artin Algebra, Prentice-Hall of India 1991
3. N.Jacobson, Basic Algebra Vols I and II Freeman 1988 ( Kalse Published by Firncustan Publishing Compay.)
4. S.Lang Algebra 3rd edition. Addison-Westely 1993
5. O.S. Luther and I.B.S. Passi, Algebra Vol. I-Groups. Vol. II-Rings, Narosa Publishing House (Vol 1-1996 Vol. II 1- 1999)
6. D.S.Malik & N.Mordeson and M.K.Sen Fundametnals of Abstract Algebra, Mc. Graw Hill International Edition, 1997
- 7.Joseph Galian , Contemporary Abstract Algebra.

**Paper No. VII**

**Paper Code: HCT 2.2**

**Real Analysis - II**

**Unit I.** Lebesgue Measure: Outer measure, Measurable sets, Lebesgue measure, non-measurable sets. ( 15L)

**Unit II.** Measurable functions: Measurable functions and their properties, Egoroff's theorem ( 15L)

**Unit III.** Lebesgue Integral: Lebesgue integral of a bounded function over a set of finite measure, the Lebesgue integral of a non-negative measurable function, Fatou's Lemma, the general Lebesgue integral, convergence in measure. ( 15L))

**Unit IV.** Differentiation and Integration: Differentiation of monotone functions, function of bounded variation, Differentiation of an integral, Absolute continuity, Convex functions. ( 15L)

**Recommended Books :**

1. Simmon G.F. : Introduction to topology and Modern Analysis, McGraw Hill Book Company, New York 1963
2. Royden H.L.: Real Analysis , Printice Hall of India.

**Reference Books :**

1. Berberian, S.K. Measure and Integration, McMillan N.Y.1965
2. Rana : An Introduction to Measure and Integration, Narosa (1997)
3. G. De. Barra, Measure and Integration

**Paper No. VIII**

**Paper Code: HCT 2.3**

**General Topology**

**Unit –I** ( 20L)

Definition and examples of topological spaces, closed sets, closure, dense sets, Neighborhood, Interior, Exterior, Boundary, accumulation points, and derived sets. Bases, subbases, Relative topology. Continuous functions and homeomorphism.

**Unit –II** ( 10 L)

Compact sets and connected sets

**Unit –III** ( 15L)

First and Second countable spaces, Lindelöf spaces, separable spaces, second countability and separability.

**Unit IV:**

Separation Axioms :  $T_0$ ,  $T_1$ ,  $T_2$ ,  $T_3$ ,  $T_{3\frac{1}{2}}$ ,  $T_4$  - Their characterizations and basic properties.

(15 L)

**Recommended Books :-**

1] Munkres J. R. :- Topology – A first course, Prentice Hall of India ( 200 )

**Reference: Books :**

1] Joshi K. D. : Introduction to General Topology – Wiley Eastern ( 1983 )

2] Willard S : General Topology, Addison Wesley ( 1970 )

3] Perwin W.J.: Foundations of General Topology, Academic Press ( 1964 )

4] Gupta K.P: Topology , Pragati Prakashan.

## Paper No. IX

### Paper Code: SCT 2.1

#### Complex Analysis

##### UNIT –I (10 L)

Cross Ratio, Mobius transformations, Analytic functions, Power series representation of analytic functions,

##### UNIT –II (20L)

Liouville's theorem, Fundamental theorem of algebra, Zeros of analytic function. Index of a closed curve, Cauchy's integral formula, Cauchy's theorem, Morera's theorem, counting zeros of analytic functions, open mapping theorem, Goursat's theorem.

##### UNIT –III (20 L)

Isolated singularities, characterization of isolated singularities, Laurent series expansion, Residues Residue theorem, Evaluation of definite integrals.

##### Unit-IV

Argument principle, Rouché's theorem, Maximum Modulus theorems, Schwarz's lemma. Hurwitz's theorem Montel theorem, Riemann mapping theorem. (10 L)

#### Recommended Books :

J.B.Conway-Function of one complex variable (second edition) Narosa (1980)

#### Reference Books :

1. L.V. Ahlfors : Complex Analysis, McGraw Hall (1979)
2. H.Silverman : Complex Variables, Hanton Mifflin (1975)
3. N.Levinson and R M.Redheffer : Complex Variables, Tata McGraw Hill (1980)
4. Remmert : Complex Function Theory, Springer Verlag
5. S.G.Kvanse : Complex Ananalysis
6. Dennis G.Zill , Patrik D. Shanahan : A first course in Complex Analysis, Jones and Bartlett Publishers.



## **Paper No.IX**

### **Paper Code: SCT 2.2**

#### **Relativistic Mechanics**

**UNIT I:Relativistic Kinematics :** (20 L)

Galilean transformations, Newtonian Relativity, Electromagnetism and Newtonian Relativity, Inertial frames, postulates of special relativity, Derivation of the Lorentz Transformation equations, Consequences of the Lorentz Transformation equations, viz. Lorentz contraction, time dilation, simultaneity and colocality of events. Invariance of electromagnetic wave equation. The relativistic addition of velocities (Einstein's formula) Lorentz velocity and acceleration transformation equations, relativistic aberration formula and Doppler effect [1]

**UNIT II:Relativistic Dynamics :** (15 L)

Variation of mass of a moving particle, relativistic momentum, force, work and energy, The equivalence of mass and energy. The transformation properties of momentum, energy, mass and force Minkowski space-time, four velocity vector, four momentum, Relativistic Lagrangian and Hamiltonian. [1]

**UNIT III :Electromagnetism :** (15 L)

The interdependence of electric and magnetic fields, The transformation for electric and magnetic fields, the field of a uniformly moving point charge, The invariance of Maxwells equations [1]

**UNIT IV: Tensor Analysis :** (10 L)

Transformation of co-ordinates, Laws of transformation of contravariant, covariant and mixed tensors of different ranks. Cartesian tensor, metric tensor.

Recommended Books :

1. Introduction to special Relativity by R.Resnick [1968]
2. "A text book of Matrix and Tensor by Paria G. Scholan's Publication, Indore.

Reference Books :

- 1.Relativity and Gravitation by Philippe Tourence (1972) Cambridge University Press.
- 2.Relativistic Mechanics by Satyaprakash , Pragati Prakashan.

**Paper No.X**

**Paper Code: OET 2.1**

**Fundamental in Mathematics**

**UNIT I:** (20 L)

Elementary Matrix Operations and Elementary Matrices, Types of Matrices and Determinants, Rank of Matrix and Matrix inverses.

**UNIT II:** (15 L)

Solutions of system of simultaneous Linear homogenous equations and Solutions of system of simultaneous linear non-homogenous equations.

**UNIT III :** (10 L)

Vector Spaces, Subspaces, Linear Combinations, Linear Dependence and Linear independence, Bases, Dimensions.

**UNIT IV:** (15 L)

Linear transformations, Null spaces, Range Spaces, Matrix representations of linear transformations.

**Recommended Books :**

1. Linear Algebra, by Stephen H. Friedberg (Author), Pearson Pub.

**Reference Books :**

1) Linear Algebra by A.R.Vasistha and J.N.Sharma (Author), Krishna Pub.

2) Linear Algebra by K.P.Gupta(Author), A Pragati Edition.

3) Joseph Gallian , Contemporary Abstract Algebra.

4) Dr. B. S. Grewal , Higher Engineering Mathematics , Khanna Publishers.

**Paper No.X**

**Paper Code: OET 2.2**

**Vedic Mathematics**

**Unit I :**

Introduction to Vedic Mathematics , First formula for multiplication , Quick formula for multiplication , importance of bases in a Quick formula . (15 L)

**Unit II :**

Criss-cross technique for multiplication by two digit numbers , Mental multiplication technique by two digit numbers. (15 L)

**Unit III :**

Real magic in division , Criss-cross technique for division , decimal division . (15 L)

**Unit IV :**

Mental formula for finding squares and cubes , finding squares of an adjacent number , tricks to find square roots and cube roots. (15 L)

**Reference Books :**

- 1) Vedic Mathematics by Pradeep Kumar , Shree publications.
- 2) Fundamentals and Applications of Vedic Mathematics , State Council Of Educational Research and Training , New Delhi.
- 3) Vedic Mathematics A fuzzy and Neutrosophic Analysis , W.B. Vasantha Kandasamy, Floretin Smarandache , Automaton Los Angeles.

**Mathematics Practical Paper-3**

**Paper Code: HCP 2.1**

**Unit – I :- Algebra II**

- 1) Problems on Extension Fields, splitting fields.
- 2) Problems on Galois theory
- 3) Problems on Constructible real numbers

**Unit – II :- Real Analysis - II**

- 1) Problems on Measurable sets.
- 2) Problems on Measurable functions.
- 3) Problems on Lebesgue differentiation and integration

**Unit – III :- Topology**

- 1) Problems on topology spaces
- 2) Problems on compact sets & connected sets
- 3) Problems on Continuous functions & homeomorphisms

**Unit – IV :- Soft Core I**

At least three practical's on this paper should be conducted.

Instruction : All practical's should be solved either by using C or C++ language.

**Mathematics Practical Paper-4**

**Paper Code: OEP 2.1**

At least ten practicals should be conducted on open elective theory paper OEP 2.1 /  
OEP 2.2.

Instruction : All practical's should be solved either by using C or C++ language.